

Aufgabenblatt Ableitungen
zur Summen- bzw. Differenzregel

Differenzialrechnung

Lösungen

Level 1 – Grundlagen – Blatt 1

Lösung A1

$$f_1(x) = x^2 + x;$$

$$f'_1(x) = 2x + 1$$

$$f_3(x) = x^3 + x^2 + x + 1;$$

$$f'_3(x) = 3x^2 + 2x + 1$$

$$f_5(x) = 2x^2 - 3x^3 + 4x^4;$$

$$f'_5(x) = 4x - 9x^2 + 16x^3$$

$$f_7(t) = 2,5t^5 + \frac{1}{t^2};$$

$$f'_7(t) = 12,5t^4 - \frac{2}{t^3}$$

$$f_2(x) = 2x^2 - x + 5;$$

$$f'_2(x) = 4x - 1$$

$$f_4(x) = -5x^4 + 3x^2;$$

$$f'_4(x) = -20x^3 + 6x$$

$$f_6(t) = \frac{1}{4}t^4 + \frac{1}{3}t^3 + \frac{1}{2}t^2;$$

$$f'_6(t) = t^3 + t^2 + t$$

Lösung A2

$$f_1(x) = x^4 + x^8;$$

$$f'_1(x) = 4x^3 + 8x^7$$

$$f_3(x) = \frac{1}{x} + x^4;$$

$$f'_3(x) = -\frac{1}{x^2 + 4x^3}$$

$$f_5(x) = \frac{1}{x} + x - 5;$$

$$f'_5(x) = -\frac{1}{x^2} + 1$$

$$f_7(t) = \sqrt{t} - t;$$

$$f'_7(t) = \frac{1}{2\sqrt{t}} - 1$$

$$f_2(x) = x^{12} + x^{-3};$$

$$f'_2(x) = 12x^{11} - 3x^{-4}$$

$$f_4(x) = \sqrt{x} - \frac{1}{x};$$

$$f'_4(x) = \frac{1}{2\sqrt{x}} + \frac{1}{x^2}$$

$$f_6(t) = \frac{2}{5}t^{-1} + 1;$$

$$f'_6(t) = -\frac{2}{5}t^{-2}$$

Lösung A3

$$f_1(x) = \frac{2}{x^{-2}} + x^2 = 3x^2;$$

$$f'_1(x) = 6x$$

$$f_2(x) = -\frac{3}{4}x^8 + 2,5x^4 - 2x + 4;$$

$$f'_2(x) = -6x^7 + 10x^3 - 2$$

$$f_3(x) = \frac{2}{9}x^3 + \frac{5}{8}x^2 + 0,4x - 1,6;$$

$$f'_3(x) = \frac{2}{3}x^2 + \frac{5}{4}x + 0,4$$

$$f_4(x) = f_4(x) = 3 \cdot \frac{1}{x} + 2x^{-3} - 5 + x^6;$$

$$f'_4(x) = -\frac{3}{x^2} - 6x^{-4} + 6x^5$$

$$f_5(x) = 4\sqrt{x} + \frac{1}{x^2} - \frac{1}{20}x^{-3} - \frac{1}{10x^{10}};$$

$$f'_5(x) = \frac{2}{\sqrt{x}} - \frac{2}{x^3} + \frac{3}{20}x^{-4} + \frac{1}{x^{11}}$$

$$f_6(t) = \frac{1}{2t} + 4\sqrt{t} - t + 1;$$

$$f'_6(t) = -\frac{1}{2t^2} + \frac{2}{\sqrt{t}} - 1$$

$$f_7(t) = \sqrt{20} \cdot t + \frac{1}{20t} + (20t)^2 - 20t;$$

$$f'_7(t) = \sqrt{20} - \frac{1}{20t^2} + 800t - 20$$